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K-Transformed Permutations

Input: Standard Input Output: Standard Output



Consider a sequence of **n** integers $<1 \ 2 \ 3 \ 4 \dots$ **n**>. Since all the values are distinct, we know that there are **n** factorial permutations. A permutation is called *K-transformed* if the absolute difference between the original position and the new position of every element is at most **K**.

Given **n** and **K**, you have to find out the total number of *K-transformed* permutations.

| Exan | nple: n = 4, K | L = 2 | |
|-----------------|------------------------------|--------------|--|
| | 1234 | <u>Valid</u> | <u>Annotation</u> |
| (position) | | | |
| \mathbf{P}_1 | 1 2 3 4 | Yes | The original sequence. All the elements are in their original |
| | | | position |
| P_2 | 1 2 4 3 | Yes | 3 and 4 are reordered, but each is shifted by 1 position only. |
| P ₃ | 1 3 2 4 | Yes | |
| P_4 | 1 3 4 2 | Yes | 2 is shifted by 2 positions. $2 \le K$, so it's a valid one. |
| P ₅ | 1 4 2 3 | Yes | |
| P ₆ | 1 4 3 2 | Yes | |
| P_7 | 2 1 3 4 | Yes | |
| P ₈ | 2 1 4 3 | Yes | |
| P ₉ | 2 3 1 4 | Yes | |
| P ₁₀ | 2 3 4 1 | No | 1 is shifted by 3 positions. $3 > K$ and so this is an invalid |
| | | | permutation |
| P ₁₁ | 2 4 1 3 | Yes | - |
| P ₁₂ | 2 4 3 1 | No | |
| P ₁₃ | 3 1 2 4 | Yes | |
| P ₁₄ | 3 1 4 2 | Yes | |
| P ₁₅ | 3 2 1 4 | Yes | |
| P ₁₆ | 3 2 4 1 | No | |
| P ₁₇ | 3 4 1 2 | Yes | |
| P ₁₈ | 3 4 2 1 | No | |
| P ₁₉ | 4 1 2 3 | No | 4 is shifted by 3 positions. $3 > K$ and so this is also invalid |
| P ₂₀ | 4 1 3 2 | No | |
| P ₂₁ | 4 2 1 3 | No | |
| P ₂₂ | 4 2 3 1 | No | |
| $P_{23}^{}$ | 4 3 1 2 | No | |
| P ₂₄ | 4 3 2 1 | No | Here, both 4 and 1 are breaking the property. |
| | | | |

So, for the above case, there are 14 2-transformed permutations.

Input

The first line of input is an integer $T(T \le 20)$ that indicates the number of test cases. Each case consists of a line containing two integers **n** and **K**. $(1 \le n \le 10^9)$ and $(0 \le K \le 3)$.

Output

For each case, output the case number first followed by the required result. Since the result could be huge, output result modulo 73405.

| Sample Input | Output for Sample Input |
|--------------|-------------------------|
| 3 | Case 1: 14 |
| 4 2 | Case 2: 1 |
| 100 0 | Case 3: 89 |
| 10 1 | |
| | |

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