

254 Towers of Hanoi

In 1883, Edouard Lucas invented, or perhaps reinvented, one of the most popular puzzles of all times – the Tower of Hanoi, as he called it – which is still used today in many computer science textbooks to demonstrate how to write a recursive algorithm or program. First of all, we will make a list of the rules of the puzzle:

- There are three pegs: A , B and C .
- There are n disks. The number n is constant while working the puzzle.
- All disks are different in size.
- The disks are initially stacked on peg A so that they increase in size from the top to the bottom.
- The goal of the puzzle is to transfer the entire tower from the A peg to one of the others pegs.
- One disk at a time can be moved from the top of a stack either to an empty peg or to a peg with a larger disk than itself on the top of its stack.

A good way to get a feeling for the puzzle is to write a program which will show a copy of the puzzle on the screen and let you simulate moving the disks around. The next step could be to write a program for solving the puzzle in a efficient way. You don't have to do neither, but only know the actual situation after a given number of moves by using a determinate algorithm.

The Algorithm

It is well known and rather easy to prove that the minimum number of moves needed to complete the puzzle with n disks is $2^n - 1$. A simple algorithm which allows us to reach this optimum is as follows: for odd moves, take the smallest disk (number 1) from the peg where it lies to the next one in the circular sequence $ABCABC\dots$; for even moves, make the only possible move not involving disk 1.

Input

The input file will consist of a series of lines. Each line will contain two integers n , m : n , lying within the range $[0, 100]$, will denote the number of disks and m , belonging to $[0, 2^n - 1]$, will be the number of the last move. The file will end at a line formed by two zeros.

Output

The output will consist again of a series of lines, one for each line of the input. Each of them will be formed by three integers indicating the number of disks in the pegs A , B and C respectively, when using the algorithm described above.

Sample Input

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3 5
64 2
8 45
0 0
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Sample Output

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1 1 1
62 1 1
4 2 2
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